

# ANSWERS

## EXERCISE 7.1

1.  $-\frac{1}{2}\cos 2x$       2.  $\frac{1}{3}\sin 3x$       3.  $\frac{1}{2}e^{2x}$
4.  $\frac{1}{3a}(ax+b)^3$       5.  $-\frac{1}{2}\cos 2x - \frac{4}{3}e^{3x}$       6.  $\frac{4}{3}e^{3x} + x + C$
7.  $\frac{x^3}{3} - x + C$       8.  $\frac{ax^3}{3} + \frac{bx^2}{2} + cx + C$       9.  $\frac{2}{3}x^3 + e^x + C$
10.  $\frac{x^2}{2} + \log|x| - 2x + C$       11.  $\frac{x^2}{2} + 5x + \frac{4}{x} + C$
12.  $\frac{2}{7}x^{\frac{7}{2}} + 2x^{\frac{3}{2}} + 8\sqrt{x} + C$       13.  $\frac{x^3}{3} + x + C$
14.  $\frac{2}{3}x^{\frac{3}{2}} - \frac{2}{5}x^{\frac{5}{2}} + C$       15.  $\frac{6}{7}x^{\frac{7}{2}} + \frac{4}{5}x^{\frac{5}{2}} + 2x^{\frac{3}{2}} + C$
16.  $x^2 - 3\sin x + e^x + C$       17.  $\frac{2}{3}x^3 + 3\cos x + \frac{10}{3}x^{\frac{3}{2}} + C$
18.  $\tan x + \sec x + C$       19.  $\tan x - x + C$
20.  $2 \tan x - 3 \sec x + C$       21. C
22. A

## EXERCISE 7.2

1.  $\log(1+x^2) + C$       2.  $\frac{1}{3}(\log|x|)^3 + C$       3.  $\log|1+\log x| + C$
4.  $\cos(\cos x) + C$       5.  $-\frac{1}{4a}\cos 2(ax+b) + C$
6.  $\frac{2}{3a}(ax+b)^{\frac{3}{2}} + C$       7.  $\frac{2}{5}(x+2)^{\frac{5}{2}} - \frac{4}{3}(x+2)^{\frac{3}{2}} + C$

8.  $\frac{1}{6}(1+2x^2)^{\frac{3}{2}} + C$     9.  $\frac{4}{3}(x^2+x+1)^{\frac{3}{2}} + C$     10.  $2\log|\sqrt{x}-1| + C$
11.  $\frac{2}{3}\sqrt{x+4}(x-8) + C$
12.  $\frac{1}{7}(x^3-1)^{\frac{7}{3}} + \frac{1}{4}(x^3-1)^{\frac{4}{3}} + C$     13.  $-\frac{1}{18(2+3x^3)^2} + C$
14.  $\frac{(\log x)^{1-m}}{1-m} + C$     15.  $-\frac{1}{8}\log|9-4x^2| + C$     16.  $\frac{1}{2}e^{2x+3} + C$
17.  $-\frac{1}{2e^{x^2}} + C$     18.  $e^{\tan^{-1}x} + C$     19.  $\log(e^x + e^{-x}) + C$
20.  $\frac{1}{2}\log(e^{2x} + e^{-2x}) + C$     21.  $\frac{1}{2}\tan(2x-3) - x + C$
22.  $-\frac{1}{4}\tan(7-4x) + C$     23.  $\frac{1}{2}(\sin^{-1}x)^2 + C$
24.  $\frac{1}{2}\log|2\sin x + 3\cos x| + C$     25.  $\frac{1}{(1-\tan x)} + C$
26.  $2\sin\sqrt{x} + C$     27.  $\frac{1}{3}(\sin 2x)^{\frac{3}{2}} + C$     28.  $2\sqrt{1+\sin x} + C$
29.  $\frac{1}{2}(\log \sin x)^2 + C$     30.  $-\log|1+\cos x| + C$     31.  $\frac{1}{1+\cos x} + C$
32.  $\frac{x}{2} - \frac{1}{2}\log|\cos x + \sin x| + C$     33.  $\frac{x}{2} - \frac{1}{2}\log|\cos x - \sin x| + C$
34.  $2\sqrt{\tan x} + C$     35.  $\frac{1}{3}(1+\log x)^3 + C$     36.  $\frac{1}{3}(x+\log x)^3 + C$
37.  $-\frac{1}{4}\cos(\tan^{-1}x^4) + C$     38. D
39. B

### EXERCISE 7.3

1.  $\frac{x}{2} - \frac{1}{8} \sin(4x+10) + C$
2.  $-\frac{1}{14} \cos 7x + \frac{1}{2} \cos x + C$
3.  $\frac{1}{4} \left[ \frac{1}{12} \sin 12x + x + \frac{1}{8} \sin 8x + \frac{1}{4} \sin 4x \right] + C$
4.  $-\frac{1}{2} \cos(2x+1) + \frac{1}{6} \cos^3(2x+1) + C$
5.  $\frac{1}{6} \cos^6 x - \frac{1}{4} \cos^4 x + C$
6.  $\frac{1}{4} \left[ \frac{1}{6} \cos 6x - \frac{1}{4} \cos 4x - \frac{1}{2} \cos 2x \right] + C$
7.  $\frac{1}{2} \left[ \frac{1}{4} \sin 4x - \frac{1}{12} \sin 12x \right] + C$
8.  $2 \tan \frac{x}{2} - x + C$
9.  $x - \tan \frac{x}{2} + C$
10.  $\frac{3x}{8} - \frac{1}{4} \sin 2x + \frac{1}{32} \sin 4x + C$
11.  $\frac{3x}{8} + \frac{1}{8} \sin 4x + \frac{1}{64} \sin 8x + C$
12.  $x - \sin x + C$
13.  $2(\sin x + x \cos \alpha) + C$
14.  $-\frac{1}{\cos x + \sin x} + C$
15.  $\frac{1}{6} \sec^3 2x - \frac{1}{2} \sec 2x + C$
16.  $\frac{1}{3} \tan^3 x - \tan x + x + C$
17.  $\sec x - \operatorname{cosec} x + C$
18.  $\tan x + C$
19.  $\log |\tan x| + \frac{1}{2} \tan^2 x + C$
20.  $\log |\cos x + \sin x| + C$
21.  $\frac{\pi x}{2} - \frac{x^2}{2} + C$
22.  $\frac{1}{\sin(a-b)} \log \left| \frac{\cos(x-a)}{\cos(x-b)} \right| + C$
23. A
24. B

### EXERCISE 7.4

1.  $\tan^{-1} x^3 + C$
2.  $\frac{1}{2} \log \left| 2x + \sqrt{1+4x^2} \right| + C$

3.  $\log \left| \frac{1}{2-x+\sqrt{x^2-4x+5}} \right| + C$
4.  $\frac{1}{5} \sin^{-1} \frac{5x}{3} + C$
5.  $\frac{3}{2\sqrt{2}} \tan^{-1} \sqrt{2} x^2 + C$
6.  $\frac{1}{6} \log \left| \frac{1+x^3}{1-x^3} \right| + C$
7.  $\sqrt{x^2-1} - \log |x+\sqrt{x^2-1}| + C$
8.  $\frac{1}{3} \log |x^3+\sqrt{x^6+a^6}| + C$
9.  $\log |\tan x + \sqrt{\tan^2 x + 4}| + C$
10.  $\log |x+1+\sqrt{x^2+2x+2}| + C$
11.  $\frac{1}{6} \tan^{-1} \left( \frac{3x+1}{2} \right) + C$
12.  $\sin^{-1} \left( \frac{x+3}{4} \right) + C$
13.  $\log \left| x - \frac{3}{2} + \sqrt{x^2-3x+2} \right| + C$
14.  $\sin^{-1} \left( \frac{2x-3}{\sqrt{41}} \right) + C$
15.  $\log \left| x - \frac{a+b}{2} + \sqrt{(x-a)(x-b)} \right| + C$
16.  $2\sqrt{2x^2+x-3} + C$
17.  $\sqrt{x^2-1} + 2 \log |x+\sqrt{x^2-1}| + C$
18.  $\frac{5}{6} \log |3x^2+2x+1| - \frac{11}{3\sqrt{2}} \tan^{-1} \left( \frac{3x+1}{\sqrt{2}} \right) + C$
19.  $6\sqrt{x^2-9x+20} + 34 \log \left| x - \frac{9}{2} + \sqrt{x^2-9x+20} \right| + C$
20.  $-\sqrt{4x-x^2} + 4 \sin^{-1} \left( \frac{x-2}{2} \right) + C$
21.  $\sqrt{x^2+2x+3} + \log |x+1+\sqrt{x^2+2x+3}| + C$
22.  $\frac{1}{2} \log |x^2-2x-5| + \frac{2}{\sqrt{6}} \log \left| \frac{x-1-\sqrt{6}}{x-1+\sqrt{6}} \right| + C$

$$23. 5\sqrt{x^2+4x+10} - 7\log|x+2+\sqrt{x^2+4x+10}| + C$$

24. B

25. B

### EXERCISE 7.5

$$1. \log \frac{(x+2)^2}{|x+1|} + C$$

$$2. \frac{1}{6} \log \left| \frac{x-3}{x+3} \right| + C$$

$$3. \log|x-1| - 5\log|x-2| + 4\log|x-3| + C$$

$$4. \frac{1}{2} \log|x-1| - 2\log|x-2| + \frac{3}{2} \log|x-3| + C$$

$$5. 4\log|x+2| - 2\log|x+1| + C$$

$$6. \frac{x}{2} + \log|x| - \frac{3}{4} \log|1-2x| + C$$

$$7. \frac{1}{2} \log|x-1| - \frac{1}{4} \log(x^2+1) + \frac{1}{2} \tan^{-1} x + C$$

$$8. \frac{2}{9} \log \left| \frac{x-1}{x+2} \right| - \frac{1}{3(x-1)} + C$$

$$9. \frac{1}{2} \log \left| \frac{x+1}{x-1} \right| - \frac{4}{x-1} + C$$

$$10. \frac{5}{2} \log|x+1| - \frac{1}{10} \log|x-1| - \frac{12}{5} \log|2x+3| + C$$

$$11. \frac{5}{3} \log|x+1| - \frac{5}{2} \log|x+2| + \frac{5}{6} \log|x-2| + C$$

$$12. \frac{x^2}{2} + \frac{1}{2} \log|x+1| + \frac{3}{2} \log|x-1| + C$$

$$13. -\log|x-1| + \frac{1}{2} \log(1+x^2) + \tan^{-1} x + C$$

$$14. 3\log|x+2| + \frac{7}{x+2} + C$$

$$15. \frac{1}{4} \log \left| \frac{x-1}{x+1} \right| - \frac{1}{2} \tan^{-1} x + C$$

$$16. \frac{1}{n} \log \left| \frac{x^n}{x^n+1} \right| + C$$

$$17. \log \left| \frac{2-\sin x}{1-\sin x} \right| + C$$

$$18. x + \frac{2}{\sqrt{3}} \tan^{-1} \frac{x}{\sqrt{3}} - 3 \tan^{-1} \frac{x}{2} + C$$

$$19. \frac{1}{2} \log \left( \frac{x^2+1}{x^2+3} \right) + C$$

$$20. \frac{1}{4} \log \left| \frac{x^4 - 1}{x^4} \right| + C$$

22. B

$$21. \log \left( \frac{e^x - 1}{e^x} \right) + C$$

23. A

### EXERCISE 7.6

1.  $-x \cos x + \sin x + C$

2.  $-\frac{x}{3} \cos 3x + \frac{1}{9} \sin 3x + C$

3.  $e^x (x^2 - 2x + 2) + C$

4.  $\frac{x^2}{2} \log x - \frac{x^2}{4} + C$

5.  $\frac{x^2}{2} \log 2x - \frac{x^2}{4} + C$

6.  $\frac{x^3}{3} \log x - \frac{x^3}{9} + C$

7.  $\frac{1}{4} (2x^2 - 1) \sin^{-1} x + \frac{x\sqrt{1-x^2}}{4} + C$

8.  $\frac{x^2}{2} \tan^{-1} x - \frac{x}{2} + \frac{1}{2} \tan^{-1} x + C$

9.  $(2x^2 - 1) \frac{\cos^{-1} x}{4} - \frac{x}{4} \sqrt{1-x^2} + C$

10.  $(\sin^{-1} x)^2 x + 2\sqrt{1-x^2} \sin^{-1} x - 2x + C$

11.  $-\sqrt{1-x^2} \cos^{-1} x + x + C$

12.  $x \tan x + \log |\cos x| + C$

13.  $x \tan^{-1} x - \frac{1}{2} \log(1+x^2) + C$

14.  $\frac{x^2}{2} (\log x)^2 - \frac{x^2}{2} \log x + \frac{x^2}{4} + C$

15.  $\left( \frac{x^3}{3} + x \right) \log x - \frac{x^3}{9} - x + C$

16.  $e^x \sin x + C$

17.  $\frac{e^x}{1+x} + C$

18.  $e^x \tan \frac{x}{2} + C$

19.  $\frac{e^x}{x} + C$

20.  $\frac{e^x}{(x-1)^2} + C$

21.  $\frac{e^{2x}}{5} (2 \sin x - \cos x) + C$

22.  $2x \tan^{-1} x - \log(1+x^2) + C$

23. A

24. B

### EXERCISE 7.7

1.  $\frac{1}{2}x\sqrt{4-x^2} + 2\sin^{-1}\frac{x}{2} + C$
2.  $\frac{1}{4}\sin^{-1}2x + \frac{1}{2}x\sqrt{1-4x^2} + C$
3.  $\frac{(x+2)}{2}\sqrt{x^2+4x+6} + \log|x+2+\sqrt{x^2+4x+6}| + C$
4.  $\frac{(x+2)}{2}\sqrt{x^2+4x+1} - \frac{3}{2}\log|x+2+\sqrt{x^2+4x+1}| + C$
5.  $\frac{5}{2}\sin^{-1}\left(\frac{x+2}{\sqrt{5}}\right) + \frac{x+2}{2}\sqrt{1-4x-x^2} + C$
6.  $\frac{(x+2)}{2}\sqrt{x^2+4x-5} - \frac{9}{2}\log|x+2+\sqrt{x^2+4x-5}| + C$
7.  $\frac{(2x-3)}{4}\sqrt{1+3x-x^2} + \frac{13}{8}\sin^{-1}\left(\frac{2x-3}{\sqrt{13}}\right) + C$
8.  $\frac{2x+3}{4}\sqrt{x^2+3x} - \frac{9}{8}\log\left|x+\frac{3}{2}+\sqrt{x^2+3x}\right| + C$
9.  $\frac{x}{6}\sqrt{x^2+9} + \frac{3}{2}\log|x+\sqrt{x^2+9}| + C$
10. A
11. D

### EXERCISE 7.8

1. 2
2.  $\log\frac{3}{2}$
3.  $\frac{64}{3}$
4.  $\frac{1}{2}$
5. 0
6.  $e^4(e-1)$
7.  $\frac{1}{2}\log 2$
8.  $\log\left(\frac{\sqrt{2}-1}{2-\sqrt{3}}\right)$
9.  $\frac{\pi}{2}$
10.  $\frac{\pi}{4}$
11.  $\frac{1}{2}\log\frac{3}{2}$
12.  $\frac{\pi}{4}$

13.  $\frac{1}{2} \log 2$

14.  $\frac{1}{5} \log 6 + \frac{3}{\sqrt{5}} \tan^{-1} \sqrt{5}$

15.  $\frac{1}{2}(e-1)$

16.  $5 - \frac{5}{2} \left( 9 \log \frac{5}{4} - \log \frac{3}{2} \right)$

17.  $\frac{\pi^4}{1024} + \frac{\pi}{2} + 2$

18. 0

19.  $3 \log 2 + \frac{3\pi}{8}$

20.  $1 + \frac{4}{\pi} - \frac{2\sqrt{2}}{\pi}$

21. D

22. C

## EXERCISE 7.9

1.  $\frac{1}{2} \log 2$

2.  $\frac{64}{231}$

3.  $\frac{\pi}{2} - \log 2$

4.  $\frac{16\sqrt{2}}{15}(\sqrt{2}+1)$

5.  $\frac{\pi}{4}$

6.  $\frac{1}{\sqrt{17}} \log \frac{21+5\sqrt{17}}{4}$

7.  $\frac{\pi}{8}$

8.  $\frac{e^2(e^2-2)}{4}$

9. D

10. B

## EXERCISE 7.10

1.  $\frac{\pi}{4}$

2.  $\frac{\pi}{4}$

3.  $\frac{\pi}{4}$

4.  $\frac{\pi}{4}$

5. 29

6. 9

7.  $\frac{1}{(n+1)(n+2)}$

8.  $\frac{\pi}{8} \log 2$

9.  $\frac{16\sqrt{2}}{15}$

10.  $\frac{\pi}{2} \log \frac{1}{2}$

11.  $\frac{\pi}{2}$

12.  $\pi$

13. 0

14. 0

15. 0

16.  $-\pi \log 2$

17.  $\frac{a}{2}$

18. 5

20. C

21. C

*MISCELLANEOUS EXERCISE ON CHAPTER 7*

1.  $\frac{1}{2} \log \left| \frac{x^2}{1-x^2} \right| + C$
2.  $\frac{2}{3(a-b)} \left[ (x+a)^{\frac{3}{2}} - (x+b)^{\frac{3}{2}} \right] + C$
3.  $-\frac{2}{a} \sqrt{\frac{(a-x)}{x}} + C$
4.  $-\left(1 + \frac{1}{x^4}\right)^{\frac{1}{4}} + C$
5.  $2\sqrt{x} - 3x^{\frac{1}{3}} + 6x^{\frac{1}{6}} - 6\log(1+x^{\frac{1}{6}}) + C$
6.  $-\frac{1}{2} \log|x+1| + \frac{1}{4} \log(x^2+9) + \frac{3}{2} \tan^{-1} \frac{x}{3} + C$
7.  $\sin a \log|\sin(x-a)| + x \cos a + C$
8.  $\frac{x^3}{3} + C$
9.  $\sin^{-1}\left(\frac{\sin x}{2}\right) + C$
10.  $-\frac{1}{2} \sin 2x + C$
11.  $\frac{1}{\sin(a-b)} \log \left| \frac{\cos(x+b)}{\cos(x+a)} \right| + C$
12.  $\frac{1}{4} \sin^{-1}(x^4) + C$
13.  $\log\left(\frac{1+e^x}{2+e^x}\right) + C$
14.  $\frac{1}{3} \tan^{-1} x - \frac{1}{6} \tan^{-1} \frac{x}{2} + C$
15.  $-\frac{1}{4} \cos^4 x + C$
16.  $\frac{1}{4} \log(x^4+1) + C$
17.  $\frac{[f(ax+b)]^{n+1}}{a(n+1)} + C$
18.  $\frac{-2}{\sin \alpha} \sqrt{\frac{\sin(x+\alpha)}{\sin x}} + C$
19.  $-2\sqrt{1-x} + \cos^{-1} \sqrt{x} + \sqrt{x-x^2} + C$
20.  $e^x \tan x + C$
21.  $-2 \log|x+1| - \frac{1}{x+1} + 3 \log|x+2| + C$
22.  $\frac{1}{2} \left[ x \cos^{-1} x - \sqrt{1-x^2} \right] + C$
23.  $-\frac{1}{3} \left(1 + \frac{1}{x^2}\right)^{\frac{3}{2}} \left[ \log\left(1 + \frac{1}{x^2}\right) - \frac{2}{3} \right] + C$

24.  $e^{\frac{\pi}{2}}$

25.  $\frac{\pi}{8}$

26.  $\frac{\pi}{6}$

27.  $2\sin^{-1}\frac{(\sqrt{3}-1)}{2}$

28.  $\frac{4\sqrt{2}}{3}$

29.  $\frac{1}{40}\log 9$

30.  $\frac{\pi}{2}-1$

31.  $\frac{19}{2}$

38. A

39. B

40. D

**EXERCISE 8.1**1.  $12\pi$ 2.  $6\pi$ 

3. A

4. B

*Miscellaneous Exercise on Chapter 8*1. (i)  $\frac{7}{3}$ 

(ii) 624.8

2. 9

3. 4

4. D

5. C

**EXERCISE 9.1**

1. Order 4; Degree not defined

2. Order 1; Degree 1

3. Order 2; Degree 1

4. Order 2; Degree not defined

5. Order 2; Degree 1

6. Order 3; Degree 2

7. Order 3; Degree 1

8. Order 1; Degree 1

9. Order 2; Degree 1

10. Order 2; Degree 1

11. D

12. A

**EXERCISE 9.2**

11. D

12. D

### EXERCISE 9.3

1.  $y = 2 \tan \frac{x}{2} - x + C$
2.  $y = 2 \sin(x + C)$
3.  $y = 1 + Ae^{-x}$
4.  $\tan x \tan y = C$
5.  $y = \log(e^x + e^{-x}) + C$
6.  $\tan^{-1} y = x + \frac{x^3}{3} + C$
7.  $y = e^{cx}$
8.  $x^{-4} + y^{-4} = C$
9.  $y = x \sin^{-1} x + \sqrt{1-x^2} + C$
10.  $\tan y = C(1 - e^x)$
11.  $y = \frac{1}{4} \log[(x+1)^2(x^2+1)^3] - \frac{1}{2} \tan^{-1} x + 1$
12.  $y = \frac{1}{2} \log\left(\frac{x^2-1}{x^2}\right) - \frac{1}{2} \log \frac{3}{4}$
13.  $\cos\left(\frac{y-2}{x}\right) = a$
14.  $y = \sec x$
15.  $2y - 1 = e^x(\sin x - \cos x)$
16.  $y - x + 2 = \log(x^2(y+2)^2)$
17.  $y^2 - x^2 = 4$
18.  $(x+4)^2 = y + 3$
19.  $(63t+27)^{\frac{1}{3}}$
20. 6.93%
21. Rs 1648
22.  $\frac{2 \log 2}{\log\left(\frac{11}{10}\right)}$
23. A

### EXERCISE 9.4

1.  $(x-y)^2 = Cx e^{\frac{-y}{x}}$
2.  $y = x \log|x| + Cx$
3.  $\tan^{-1}\left(\frac{y}{x}\right) = \frac{1}{2} \log(x^2 + y^2) + C$
4.  $x^2 + y^2 = Cx$
5.  $\frac{1}{2\sqrt{2}} \log\left|\frac{x+\sqrt{2}y}{x-\sqrt{2}y}\right| = \log|x| + C$
6.  $y + \sqrt{x^2 + y^2} = Cx^2$
7.  $xy \cos\left|\frac{y}{x}\right| = C$
8.  $x \left[1 - \cos\left(\frac{y}{x}\right)\right] = C \sin\left(\frac{y}{x}\right)$

9.  $cy = \log \left| \frac{y}{x} \right| - 1$

10.  $ye^{\frac{x}{y}} + x = C$

11.  $\log(x^2 + y^2) + 2 \tan^{-1} \frac{y}{x} = \frac{\pi}{2} + \log 2$

12.  $y + 2x = 3x^2 y$

13.  $\cot\left(\frac{y}{x}\right) = \log|ex|$

14.  $\cos\left(\frac{y}{x}\right) = \log|ex|$

15.  $y = \frac{2x}{1 - \log|x|} \quad (x \neq 0, x \neq e)$

16. C

17. D

**EXERCISE 9.5**

1.  $y = \frac{1}{5}(2\sin x - \cos x) + C e^{-2x}$

2.  $y = e^{-2x} + C e^{-3x}$

3.  $xy = \frac{x^4}{4} + C$

4.  $y(\sec x + \tan x) = \sec x + \tan x - x + C$

5.  $y = (\tan x - 1) + C e^{-\tan x}$

6.  $y = \frac{x^2}{16}(4\log|x| - 1) + C x^{-2}$

7.  $y \log x = \frac{-2}{x}(1 + \log|x|) + C$

8.  $y = (1+x)^{-1} \log|\sin x| + C(1+x^2)^{-1}$

9.  $y = \frac{1}{x} - \cot x + \frac{C}{x \sin x}$

10.  $(x + y + 1) = C e^y$

11.  $x = \frac{y^2}{3} + \frac{C}{y}$

12.  $x = 3y^2 + Cy$

13.  $y = \cos x - 2 \cos^2 x$

14.  $y(1 + x^2) = \tan^{-1} x - \frac{\pi}{4}$

15.  $y = 4 \sin^3 x - 2 \sin^2 x$

16.  $x + y + 1 = e^x$

17.  $y = 4 - x - 2 e^x$

18. C

19. D

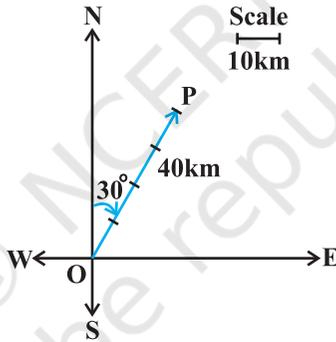
**Miscellaneous Exercise on Chapter 9**

1. (i) Order 2; Degree 1      (ii) Order 1; Degree 3  
 (iii) Order 4; Degree not defined

4.  $\sin^{-1}y + \sin^{-1}x = C$
6.  $\cos y = \frac{\sec x}{\sqrt{2}}$
7.  $\tan^{-1}y + \tan^{-1}(e^x) = \frac{\pi}{2}$
8.  $e^{\frac{x}{y}} = y + C$
9.  $\log|x-y| = x + y + 1$
10.  $ye^{2\sqrt{x}} = (2\sqrt{x} + C)$
11.  $y \sin x = 2x^2 - \frac{\pi^2}{2}$  ( $\sin x \neq 0$ )
12.  $y = \log \left| \frac{2x+1}{x+1} \right|, x \neq -1$
13. C
14. C
15. C

### EXERCISE 10.1

1. In the adjoining figure, the vector  $\overline{OP}$  represents the required displacement.



2. (i) scalar (ii) vector (iii) scalar (iv) scalar (v) scalar  
(vi) vector
3. (i) scalar (ii) scalar (iii) vector (iv) vector (v) scalar
4. (i) Vectors  $\vec{a}$  and  $\vec{b}$  are cointial  
(ii) Vectors  $\vec{b}$  and  $\vec{d}$  are equal  
(iii) Vectors  $\vec{a}$  and  $\vec{c}$  are collinear but not equal
5. (i) True (ii) False (iii) False (iv) False

### EXERCISE 10.2

1.  $|\vec{a}| = \sqrt{3}, |\vec{b}| = \sqrt{62}, |\vec{c}| = 1$
2. An infinite number of possible answers.

3. An infinite number of possible answers.

4.  $x = 2, y = 3$

5.  $-7$  and  $6; -7\hat{i}$  and  $6\hat{j}$

6.  $-4\hat{j} - \hat{k}$

7.  $\frac{1}{\sqrt{6}}\hat{i} + \frac{1}{\sqrt{6}}\hat{j} + \frac{2}{\sqrt{6}}\hat{k}$

8.  $\frac{1}{\sqrt{3}}\hat{i} + \frac{1}{\sqrt{3}}\hat{j} + \frac{1}{\sqrt{3}}\hat{k}$

9.  $\frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{k}$

10.  $\frac{40}{\sqrt{30}}\hat{i} - \frac{8}{\sqrt{30}}\hat{j} + \frac{16}{\sqrt{30}}\hat{k}$

12.  $\frac{1}{\sqrt{14}}, \frac{2}{\sqrt{14}}, \frac{3}{\sqrt{14}}$

13.  $-\frac{1}{3}, -\frac{2}{3}, \frac{2}{3}$

15. (i)  $-\frac{1}{3}\hat{i} + \frac{4}{3}\hat{j} + \frac{1}{3}\hat{k}$  (ii)  $-3\hat{i} + 3\hat{k}$

16.  $3\hat{i} + 2\hat{j} + \hat{k}$

18. (C)

19. (B), (C), (D)

### EXERCISE 10.3

1.  $\frac{\pi}{4}$

2.  $\cos^{-1}\left(\frac{5}{7}\right)$

3. 0

4.  $\frac{60}{\sqrt{114}}$

6.  $\frac{16\sqrt{2}}{3\sqrt{7}}, \frac{2\sqrt{2}}{3\sqrt{7}}$

7.  $6|\vec{a}|^2 + 11\vec{a} \cdot \vec{b} - 35|\vec{b}|^2$

8.  $|\vec{a}|=1, |\vec{b}|=1$

9.  $\sqrt{13}$

10. 8

12. Vector  $\vec{b}$  can be any vector

13.  $-\frac{3}{2}$

14. Take any two non-zero perpendicular vectors  $\vec{a}$  and  $\vec{b}$

15.  $\cos^{-1}\left(\frac{10}{\sqrt{102}}\right)$

18. (D)

### EXERCISE 10.4

1.  $19\sqrt{2}$

2.  $\pm\frac{2}{3}\hat{i}, \frac{2}{3}\hat{j}, \frac{1}{3}\hat{k}$

3.  $\frac{\pi}{3}, \frac{1}{2}, \frac{1}{\sqrt{2}}, \frac{1}{2}$

5.  $3, \frac{27}{2}$

6. Either  $|\vec{a}|=0$  or  $|\vec{b}|=0$

8. No; take any two nonzero collinear vectors

9.  $\frac{\sqrt{61}}{2}$

10.  $15\sqrt{2}$

11. (B)

12. (C)

### Miscellaneous Exercise on Chapter 10

1.  $\frac{\sqrt{3}}{2}\hat{i} + \frac{1}{2}\hat{j}$

2.  $x_2 - x_1, y_2 - y_1, z_2 - z_1; \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$

3.  $\frac{-5}{2}\hat{i} + \frac{3\sqrt{3}}{2}\hat{j}$

4. No; take  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  to represent the sides of a triangle.

5.  $\pm \frac{1}{\sqrt{3}}$

6.  $\frac{3}{2}\sqrt{10}\hat{i} + \frac{\sqrt{10}}{2}\hat{j}$

7.  $\frac{3}{\sqrt{22}}\hat{i} - \frac{3}{\sqrt{22}}\hat{j} + \frac{2}{\sqrt{22}}\hat{k}$

8. 2 : 3

9.  $3\vec{a} + 5\vec{b}$

10.  $\frac{1}{7}(3\hat{i} - 6\hat{j} + 2\hat{k}); 11\sqrt{5}$

12.  $\frac{1}{3}(160\hat{i} - 5\hat{j} + 70\hat{k})$

13.  $\lambda = 1$

16. (B)

17. (D)

18. (C)

19. (B)

#### EXERCISE 11.1

1.  $0, \frac{-1}{\sqrt{2}}, \frac{1}{\sqrt{2}}$

2.  $\pm \frac{1}{\sqrt{3}}, \pm \frac{1}{\sqrt{3}}, \pm \frac{1}{\sqrt{3}}$

3.  $\frac{-9}{11}, \frac{6}{11}, \frac{-2}{11}$

5.  $\frac{-2}{\sqrt{17}}, \frac{-2}{\sqrt{17}}, \frac{3}{17}; \frac{-2}{\sqrt{17}}, \frac{-3}{\sqrt{17}}, \frac{-2}{\sqrt{17}}; \frac{4}{\sqrt{42}}, \frac{5}{\sqrt{42}}, \frac{-1}{\sqrt{42}}$

#### EXERCISE 11.2

4.  $\vec{r} = \hat{i} + 2\hat{j} + 3\hat{k} + \lambda(3\hat{i} + 2\hat{j} - 2\hat{k})$ , where  $\lambda$  is a real number

5.  $\vec{r} = 2\hat{i} - \hat{j} + 4\hat{k} + \lambda(\hat{i} + 2\hat{j} - \hat{k})$  and cartesian form is

$$\frac{x-2}{1} = \frac{y+1}{2} = \frac{z-4}{-1}$$

$$6. \frac{x+2}{3} = \frac{y-4}{5} = \frac{z+5}{6}$$

$$7. \vec{r} = (5\hat{i} - 4\hat{j} + 6\hat{k}) + \lambda(3\hat{i} + 7\hat{j} + 2\hat{k})$$

$$8. \text{(i) } \theta = \cos^{-1}\left(\frac{19}{21}\right) \quad \text{(ii) } \theta = \cos^{-1}\left(\frac{8}{5\sqrt{3}}\right)$$

$$9. \text{(i) } \theta = \cos^{-1}\left(\frac{26}{9\sqrt{38}}\right) \quad \text{(ii) } \theta = \cos^{-1}\left(\frac{2}{3}\right)$$

$$10. p = \frac{70}{11}$$

$$12. \frac{3\sqrt{2}}{2}$$

$$13. 2\sqrt{29}$$

$$14. \frac{3}{\sqrt{19}}$$

$$15. \frac{8}{\sqrt{29}}$$

### Miscellaneous Exercise on Chapter 11

$$1. 90^\circ$$

$$2. \frac{x}{1} = \frac{y}{0} = \frac{z}{0}$$

$$3. k = \frac{-10}{7}$$

$$4. 9$$

$$5. \vec{r} = \hat{i} + 2\hat{j} - 4\hat{k} + \lambda(2\hat{i} + 3\hat{j} + 6\hat{k})$$

### EXERCISE 12.1

$$1. \text{ Maximum } Z = 16 \text{ at } (0, 4)$$

$$2. \text{ Minimum } Z = -12 \text{ at } (4, 0)$$

$$3. \text{ Maximum } Z = \frac{235}{19} \text{ at } \left(\frac{20}{19}, \frac{45}{19}\right)$$

$$4. \text{ Minimum } Z = 7 \text{ at } \left(\frac{3}{2}, \frac{1}{2}\right)$$

$$5. \text{ Maximum } Z = 18 \text{ at } (4, 3)$$

$$6. \text{ Minimum } Z = 6 \text{ at all the points on the line segment joining the points } (6, 0) \text{ and } (0, 3).$$

7. Minimum  $Z = 300$  at  $(60, 0)$ ;  
Maximum  $Z = 600$  at all the points on the line segment joining the points  $(120, 0)$  and  $(60, 30)$ .
8. Minimum  $Z = 100$  at all the points on the line segment joining the points  $(0, 50)$  and  $(20, 40)$ ;  
Maximum  $Z = 400$  at  $(0, 200)$
9.  $Z$  has no maximum value
10. No feasible region, hence no maximum value of  $Z$ .

### EXERCISE 13.1

1.  $P(E|F) = \frac{2}{3}$ ,  $P(F|E) = \frac{1}{3}$
2.  $P(A|B) = \frac{16}{25}$
3. (i) 0.32                      (ii) 0.64                      (iii) 0.98
4.  $\frac{11}{26}$
5. (i)  $\frac{4}{11}$                       (ii)  $\frac{4}{5}$                       (iii)  $\frac{2}{3}$
6. (i)  $\frac{1}{2}$                       (ii)  $\frac{3}{7}$                       (iii)  $\frac{6}{7}$
7. (i) 1                      (ii) 0
8.  $\frac{1}{6}$                       9. 1                      10. (a)  $\frac{1}{3}$ , (b)  $\frac{1}{9}$
11. (i)  $\frac{1}{2}, \frac{1}{3}$                       (ii)  $\frac{1}{2}, \frac{2}{3}$                       (iii)  $\frac{3}{4}, \frac{1}{4}$
12. (i)  $\frac{1}{2}$                       (ii)  $\frac{1}{3}$                       13.  $\frac{5}{9}$
14.  $\frac{1}{15}$                       15. 0                      16. C                      17. D

**EXERCISE 13.2**

1.  $\frac{3}{25}$                       2.  $\frac{25}{102}$                       3.  $\frac{44}{91}$
4. A and B are independent                      5. A and B are not independent
6. E and F are not independent
7. (i)  $p = \frac{1}{10}$                       (ii)  $p = \frac{1}{5}$
8. (i) 0.12                      (ii) 0.58                      (iii) 0.3                      (iv) 0.4
9.  $\frac{3}{8}$                       10. A and B are not independent
11. (i) 0.18                      (ii) 0.12                      (iii) 0.72                      (iv) 0.28
12.  $\frac{7}{8}$                       13. (i)  $\frac{16}{81}$ , (ii)  $\frac{20}{81}$ , (iii)  $\frac{40}{81}$
14. (i)  $\frac{2}{3}$ , (ii)  $\frac{1}{2}$                       15. (i), (ii)                      16. (a)  $\frac{1}{5}$ , (b)  $\frac{1}{3}$ , (c)  $\frac{1}{2}$
17. D                      18. B

**EXERCISE 13.3**

1.  $\frac{1}{2}$                       2.  $\frac{2}{3}$                       3.  $\frac{9}{13}$                       4.  $\frac{12}{13}$
5.  $\frac{22}{133}$                       6.  $\frac{4}{9}$                       7.  $\frac{1}{52}$                       8.  $\frac{1}{4}$
9.  $\frac{2}{9}$                       10.  $\frac{8}{11}$                       11.  $\frac{5}{34}$                       12.  $\frac{11}{50}$
13. A                      14. C

*Miscellaneous Exercise on Chapter 13*

1. (i) 1                      (ii) 0
2. (i)  $\frac{1}{3}$                       (ii)  $\frac{1}{2}$
3.  $\frac{20}{21}$

$$4. 1 - \sum_{r=7}^{10} {}^{10}C_r (0.9)^r (0.1)^{10-r}$$

$$5. \frac{2}{7}$$

$$6. \frac{1}{15}, \frac{2}{5}, \frac{8}{15}$$

$$7. \frac{14}{29}$$

$$8. \frac{3}{16}$$

$$9. \text{(i) } 0.5 \quad \text{(ii) } 0.05$$

$$10. \frac{16}{31}$$

$$11. A$$

$$12. C$$

$$13. B$$



© NCERT  
not to be republished

## Notes

---

© NCERT  
not to be republished